## Canguro Matemático



Junior Test
Tenth and eleventh grades

Kangourou Sans Frontières

Costa Rica 2016

9 and 12?	( <b>D</b> ) 0	( <b>G</b> ) 0	( <b>D</b> ) 10	( <b>E</b> ) 2 <i>C</i>
$(\mathbf{A})$ 0	(B) 8	( <b>C</b> ) 9	( <b>D</b> ) 10	$(\mathbf{E})$ 36
2. Which of t	he following numbe	rs is the closest to t	he result of $\frac{17 \times}{}$	$\frac{0.3 \times 20.16}{999}$ ?
(A) 0.01	(B) 0.1	$(\mathbf{C})$ 1	( <b>D</b> ) 10	(E) 100
answers. Each		right or wrong. How	_	ers than she had wrong nswers did Ruth have
( <b>A</b> ) 10	<b>(B)</b> 12	(C) 15	( <b>D</b> ) 18	(E) 20
point is not a v	ertex of this square	?		es of a square. Which
point is not a v	ertex of this square			
point is not a v $(\mathbf{A}) (-1; 3)$	rertex of this square $(\mathbf{B}) \ (0; -4)$ positive integer $x$ in	? (C) $(-2; -1)$	$(\mathbf{D}) (1;1)$	
point is not a v $(\mathbf{A}) (-1; 3)$ <b>5.</b> When the when $3x$ is divi	rertex of this square $(\mathbf{B}) \ (0; -4)$ positive integer $x$ in	? (C) $(-2; -1)$ s divided by 6, the	$(\mathbf{D}) (1;1)$	$(\mathbf{E})\ (3;-2)$
point is not a vector $(\mathbf{A})$ $(-1;3)$ 5. When the when $3x$ is divided $(\mathbf{A})$ 4	rertex of this square $(\mathbf{B}) (0; -4)$ positive integer $x$ ided by 6?	? (C) (-2; -1) s divided by 6, the (C) 2	( <b>D</b> ) (1; 1) remainder is 3.	( <b>E</b> ) $(3; -2)$ What is the remainder
<ul> <li>(A) (-1; 3)</li> <li>5. When the when 3x is divi</li> <li>(A) 4</li> <li>6. How many</li> </ul>	rertex of this square $(\mathbf{B}) \ (0; -4)$ $(\mathbf{B}) \ (0; -4)$ $(\mathbf{B}) \ (0; -4)$ $(\mathbf{B}) \ (0; -4)$ $(\mathbf{B}) \ 3$ $(\mathbf{B}) \ 3$ $(\mathbf{B}) \ 3$	? (C) (-2; -1) s divided by 6, the (C) 2	( <b>D</b> ) (1; 1) remainder is 3. ( <b>D</b> ) 1	( <b>E</b> ) $(3; -2)$ What is the remainder ( <b>E</b> ) $0$
<ul> <li>(A) (-1; 3)</li> <li>5. When the when 3x is divi</li> <li>(A) 4</li> <li>6. How many</li> <li>(A) 6</li> <li>7. Little Luca usual way with</li> </ul>	rertex of this square  (B) (0; -4)  positive integer x is ded by 6?  (B) 3  weeks are the same  (B) 8  as invented his own the negative sign is	? (C) (-2; -1)  s divided by 6, the (C) 2  e as 2016 hours? (C) 10  way to write down	(D) (1; 1) remainder is 3.  (D) 1  (D) 12  negative numbers packwards, he'd wards	(E) $(3; -2)$ What is the remainder (E) $0$

 $\bf 9.~~$  How many times do two directly adjacent letters have to be exchanged in order to change the word VELO step by step into the word LOVE ?

numbers are negative (-1, -3, -5) in place of (-1, 3, 5). If I throw TWO such dice, which of these

 $(\mathbf{D})$  7

 $(\mathbf{E})$  8

e word VELO step by step into the word LOVE?

**(A)** 3 **(B)** 4 **(C)** 5 **(D)** 6 **(E)** 7

 $(\mathbf{C})$  5

totals can not be achieved?

 $(\mathbf{B}) 4$ 

 $(\mathbf{A})$  3

10. Sven wrote five different one-digit positive integers on a blackboard. He discovered that no sum of any two numbers is equal to 10. Which of the following numbers did Sven definitely write on the blackboard?

- $(\mathbf{A})$  1
- $(\mathbf{B})$  2
- $(\mathbf{C})$  3
- **(D)** 4
- $(\mathbf{E})$  5

4 points

11. Let  $a+5=b^2-1=c^2+3=d-4$ . Which one of the numbers a, b, c, d is the largest?

 $(\mathbf{A}) a$ 

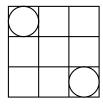
**(B)** *b* 

 $(\mathbf{C}) c$ 

**(D)** *d* 

(E) impossible to determine

The  $3 \times 3$  table is divided into 9 unit squares, and two circles are inscribed in two of them (see picture). What is the distance between the two circles?



- **(A)**  $2\sqrt{2} 1$  **(B)**  $\sqrt{2} + 1$  **(C)**  $2\sqrt{2}$

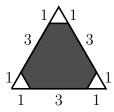
- $(\mathbf{D})$  2
- $(\mathbf{E})$  3

13. In a tennis tournament on a knock-out basis, six of the results of the quarter-finals, the semi-finals and the final were (not necessarily in this order): Bella beat Ann, Celine beat Donna, Gina beat Holly, Gina beat Celine, Celine beat Bella and Emma beat Farah. Which result is missing?

- (A) Gina beat Bella
- (B) Celine beat Ann
- (C) Emma beat Celine

- (**D**) Bella beat Holly
- (E) Gina beat Emma

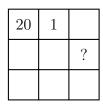
14. What percent of the area of the triangle is shaded in the figure?



- (A) 80%
- (B) 85%
- (C) 88%
- $(\mathbf{D}) 90\%$

(E) impossible to determine

**15.** Jill is making a magic multiplication square using the numbers 1, 2, 4, 5, 10, 20, 25, 50 and 100. The products of the numbers in each row, in each column and in the two diagonals should all be the same. In the figure you can see how she has started. Which number should Jill place in the cell with the question mark?



 $(\mathbf{A})$  2

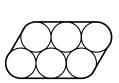
**(B)** 4

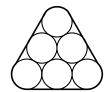
(C) 5

(**D**) 10

(E) 25

16. Jack wants to hold six circular pipes with diameter 2 cm together by a rubber band. He decided between two options as shown in the picture. Compare the lengths of the rubber bands.





(A) In the left picture it is  $\pi$  cm shorter.

(B) In the left picture it is 4 cm shorter.

(C) In the right picture it is  $\pi$  cm shorter.

(**D**) In the right picture it is 4 cm shorter.

 $(\mathbf{E})$  Both have the same length.

17. Eight unmarked envelopes contain the numbers: 1, 2, 4, 8, 16, 32, 64, 128. Eve chooses a few envelopes randomly. Alie takes the rest. Both sum up their numbers. Eve's sum is 31 more than Alie's. How many envelopes did Eve take?

(A) 2

 $(\mathbf{B}) 3$ 

(C) 4

 $(\mathbf{D})$  5

 $(\mathbf{E})$  6

18. Peter wants to colour the cells of a  $3 \times 3$  square in such a way that each of the rows, the columns and both diagonals have three cells of three different colours. What is the least number of colours Peter could use?



 $(\mathbf{A})$  3

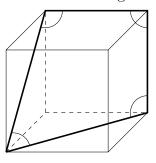
**(B)** 4

(C) 5

 $(\mathbf{D})$  6

 $(\mathbf{E})$  7

19. The picture shows a cube with four marked angles. What is the sum of these angles?



- **(A)**  $315^{\circ}$
- **(B)**  $330^{\circ}$
- (C)  $345^{\circ}$
- **(D)**  $360^{\circ}$
- **(E)**  $375^{\circ}$

**20.** There are 2016 kangaroos, each of them is either grey or red and at least one of them is grey and at least one is red. For every kangaroo K we compute the fraction of the number of kangaroos of the other colour divided by the number of kangaroos of the same colour as K (including K). Find the sum of the fractions of all 2016 kangaroos.

(A) 2016

**(B)** 1344

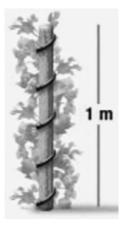
(C) 1008

(D) 672

(E) more information is needed

5 points

21. A plant wound itself exactly 5 times around a pole with height 1 m and circumference 15 cm as shown in the picture. As it climbed, its height increased at a constant rate. What is the length of the plant?

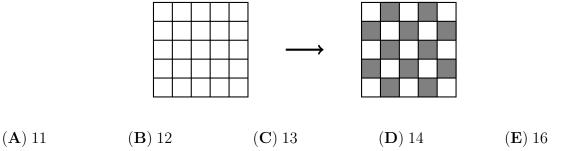


- (A) 0.75 m
- (B) 1.0 m
- (C) 1.25 m
- (**D**) 1.5 m
- (E) 1.75 m

**22.** What is the largest possible remainder that can be obtained when a two-digit number is divided by the sum of its digits?

- (**A**) 13
- (B) 14
- (C) 15
- (**D**) 16
- (E) 17

23. A  $5 \times 5$  square is divided into 25 cells. Initially all its cells are white, as shown on the left. Neighbouring cells are those that share a common edge. On each move you can choose two neighbouring cells soy they have their colours changed to the opposite colour (e.g. white cells become black and black ones become white). What is the minimum number of moves required in order to obtain the chess-like colouring shown on the right?



**24.** It takes 4 hours for a motorboat to travel downstream from X to Y. To return upstream from Y to X it takes the motorboat 6 hours. How many hours would it take a wooden log to be carried from X to Y by the current, assuming it is unhindered by any obstacles?

(**D**) 20

(E) 24

- **25.** In the Kangaroo republic each month consists of 40 days, numbered 1 to 40. Any day whose number is divisible by 6 is a holiday, and any day whose number is a prime is a holiday.
  - **(A)** 1 **(B)** 2 **(C)** 3 **(D)** 4 **(E)** 5

How many times in a month does a single working day occur between two holidays?

(C) 12

 $(\mathbf{A})$  5

(**B**) 10

- **26.** Two of the altitudes of a triangle are 10 cm and 11 cm. Which of the following cannot be the length of the third altitude?
  - (A) 5 cm (B) 6 cm (C) 7 cm (D) 10 cm (E) 100 cm
- **27.** Jakob wrote down four consecutive positive integers. He then calculated the four possible totals made by taking three of the integers at a time. None of these totals was a prime. What is the smallest integer Jakob could have written?
  - (A) 12 (B) 10 (C) 7 (D) 6 (E) 3
- 28. Four sportsmen and sportswomen —a skier, a speed skater, a hockey player and a snowboarder— had dinner at a round table. The skier sat at Andrea's left hand. The speed skater sat opposite Ben. Eva and Filip sat next to each other. A woman sat at the hockey player's left hand. Which sport did Eva do?
  - (A) speed skating (B) skiing (C) ice hockey (D) snowboarding
  - $(\mathbf{E})$  It's not possible to find out with the given information.

29. Dates can be written in the form DD.MM.YYYY. For example, today's date is 17.03.2016. A date is called "surprising" if all 8 digits in its written form are different. In what month will

the next surprising date occur?

$(\mathbf{A})$ March	$(\mathbf{B})$ June	$(\mathbf{C})$ July	$(\mathbf{D})$ August	$(\mathbf{E})$ December		
from P1 to P2	015 shook hands wi	th exactly the sai		016. Each participan cipants as the one of shake?		
$(\mathbf{A})\ 1$	(B) 504	(C) 672	$(\mathbf{D})\ 1008$	$(\mathbf{E})\ 2015$		



## Answers

Name:_												
Institution:					Gra	Grade:						
01.	A	В	С	D	Е	16.	A	В	С	D	Е	
02.	A	В	С	D	Е	17.	A	В	С	D	Е	
03.	A	В	С	D	Е	18.	A	В	С	D	Е	
04.	A	В	С	D	Е	19.	A	В	С	D	Е	
05.	A	В	С	D	Е	20.	A	В	С	D	Е	
06.	A	В	С	D	Е	21.	A	В	С	D	Е	
07.	A	В	С	D	Е	22.	A	В	С	D	Е	
08.	A	В	С	D	Е	23.	A	В	С	D	Е	
09.	A	В	С	D	Е	24.	A	В	С	D	Е	
10.	A	В	С	D	Е	25.	A	В	С	D	Е	
11.	A	В	С	D	Е	26.	A	В	С	D	Е	
12.	A	В	С	D	Е	27.	A	В	С	D	Е	
13.	A	В	С	D	Е	28.	A	В	С	D	Е	
14.	A	В	С	D	Е	29.	A	В	С	D	Е	
15.	A	В	С	D	Е	30.	A	В	С	D	Е	